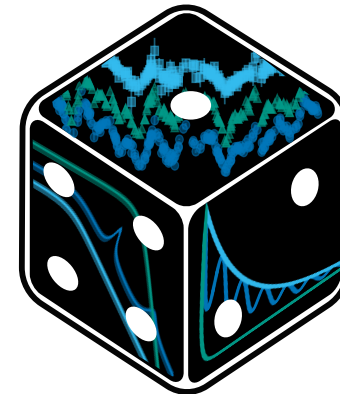
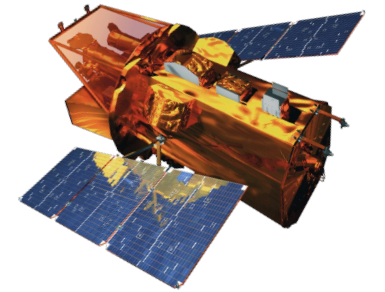
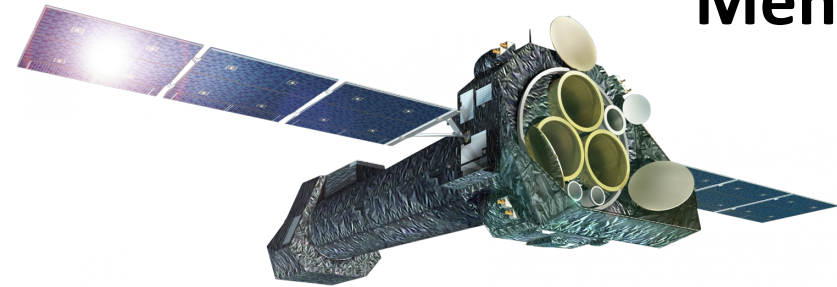


# Next generation timing method for irregular light curves of AGN

**Mehdy Lefkir** – 2<sup>nd</sup> year PhD student

ml556@leicester.ac.uk

Supervisor: Simon Vaughan



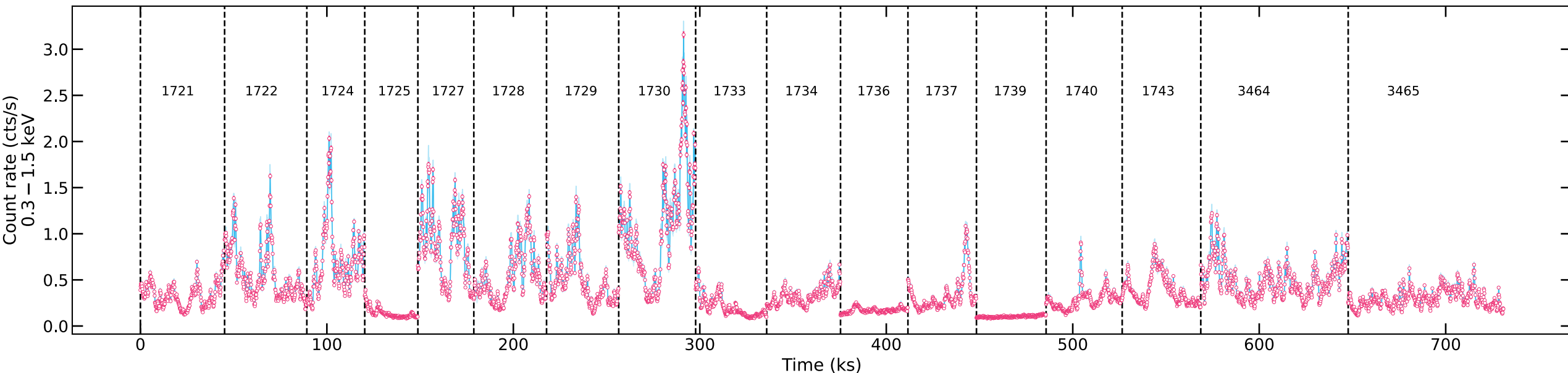
UNIVERSITY OF  
**LEICESTER**

XMM-Newton survey legacy for Athena and beyond- 27<sup>th</sup> Feb. 2024 - Toulouse

# Motivations

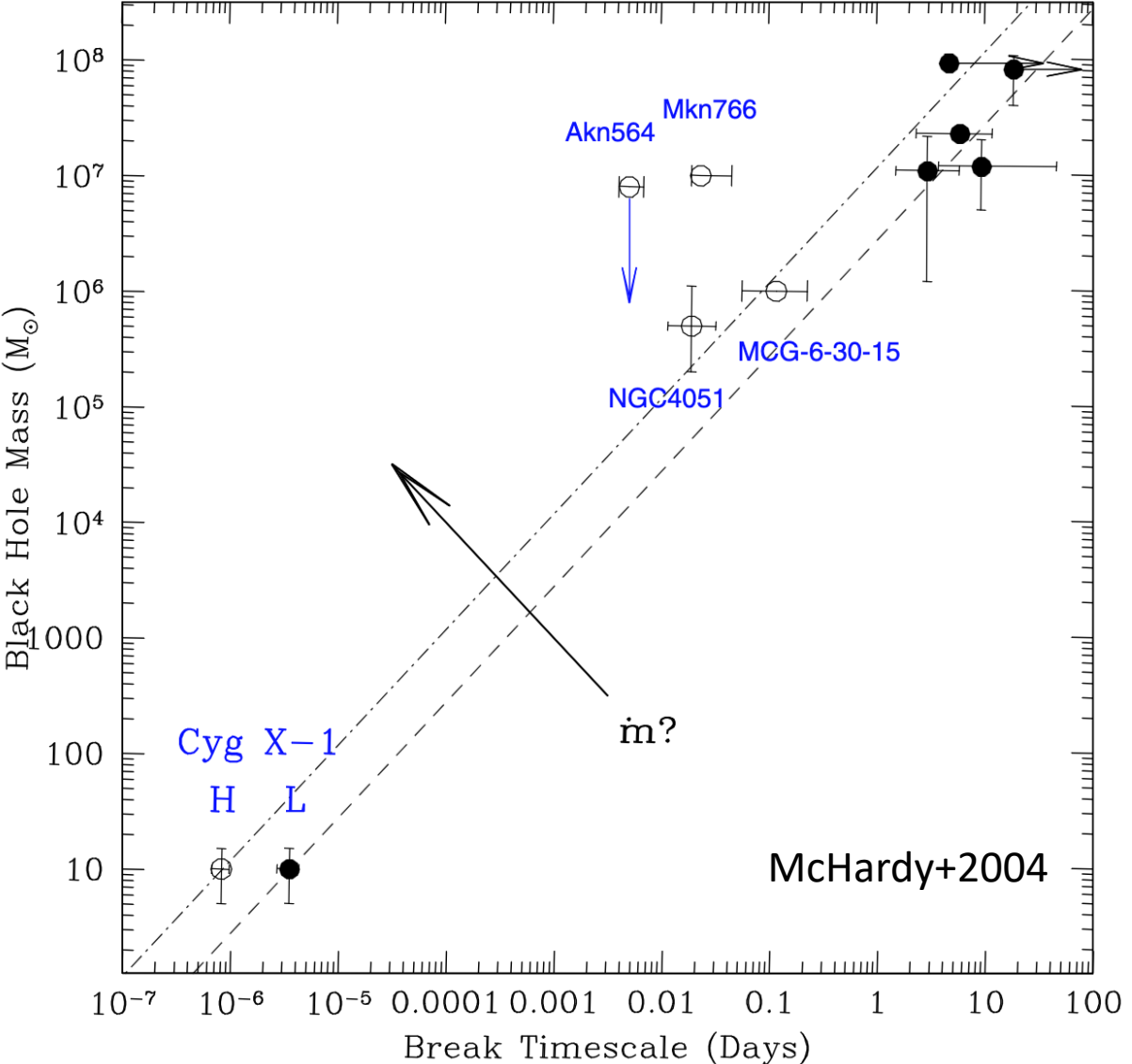
- unobscured AGN show a strong variability, what is the physical origin of the variability ?
- Study correlations/delays between wavebands to test models of reprocessing and structure of the engine

## XMM-Newton observations of NGC 4051



# Motivations

- unobscured AGN show a strong variability, what is the physical origin of the variability ?
- Study correlations/delays between wavebands to test models of reprocessing and structure of the engine
- Estimate the shape of power spectrum of several AGN using data from RXTE, Swift, XMM-Newton, ASCA...

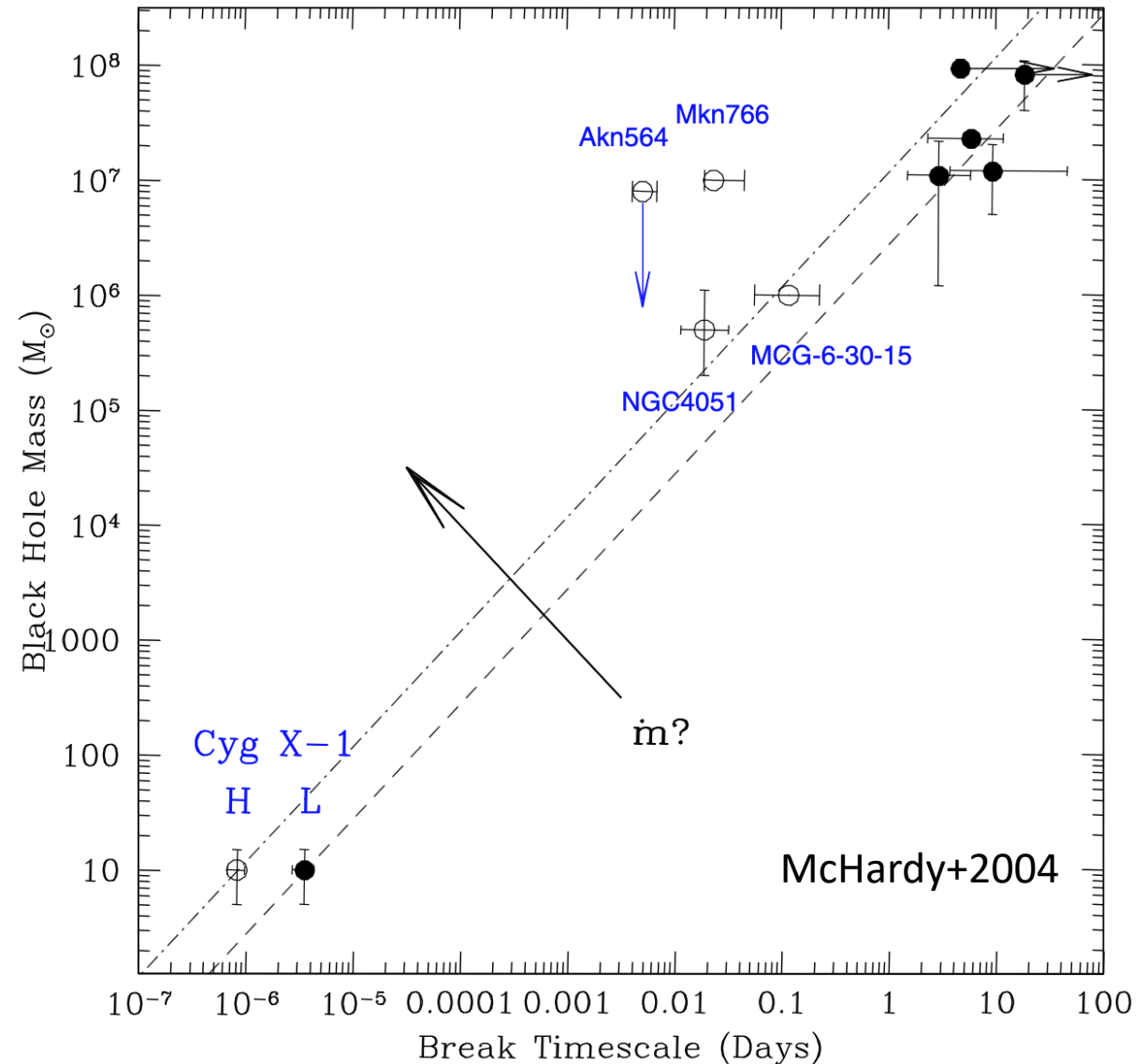


# Motivations

- unobscured AGN show a strong variability, what is the physical origin of the variability ?
- Study correlations/delays between wavebands to test models of reprocessing and structure of the engine
- Estimate the shape of the power spectrum of several AGN using data from RXTE, Swift, XMM-Newton, ASCA...

We need a method which can cope with:

- irregular sampling, gaps
- uncertainties on measurement
- leakage and aliasing



# Gaussian process regression

Rasmussen & Williams, 2006

A nice and easy way to interpolate points **assuming** the joint probability density function is Gaussian.

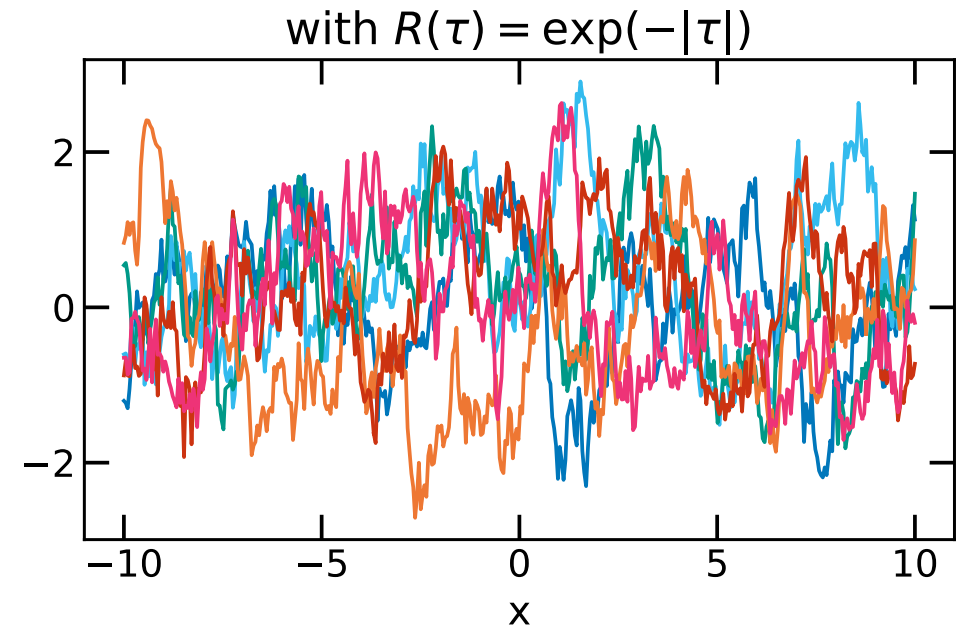
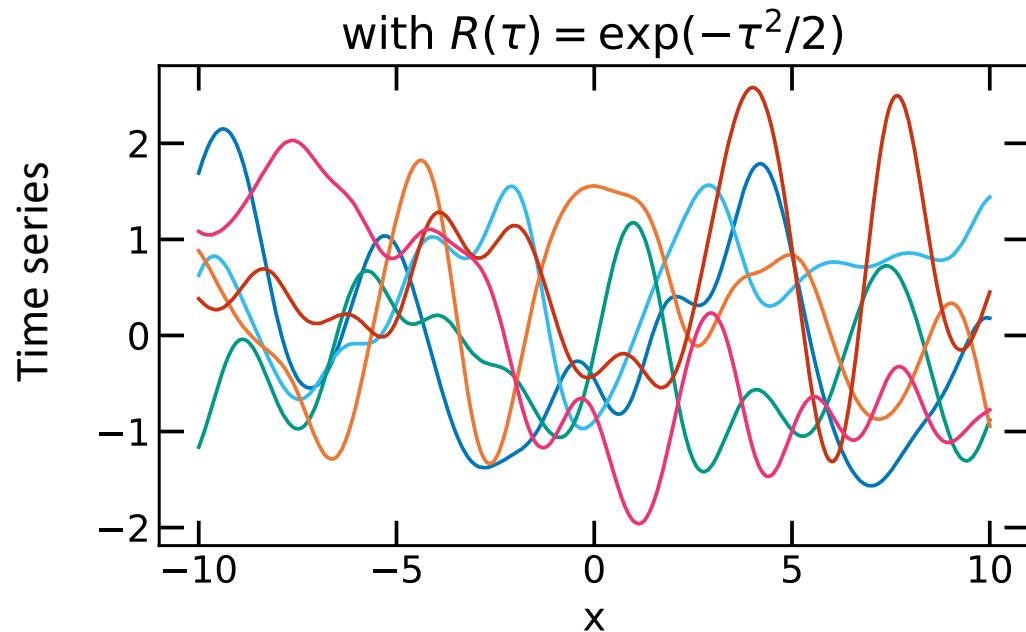
A GP is described by a **mean** function and a **covariance** function (or **autocovariance**)

# Gaussian process regression

Rasmussen & Williams, 2006

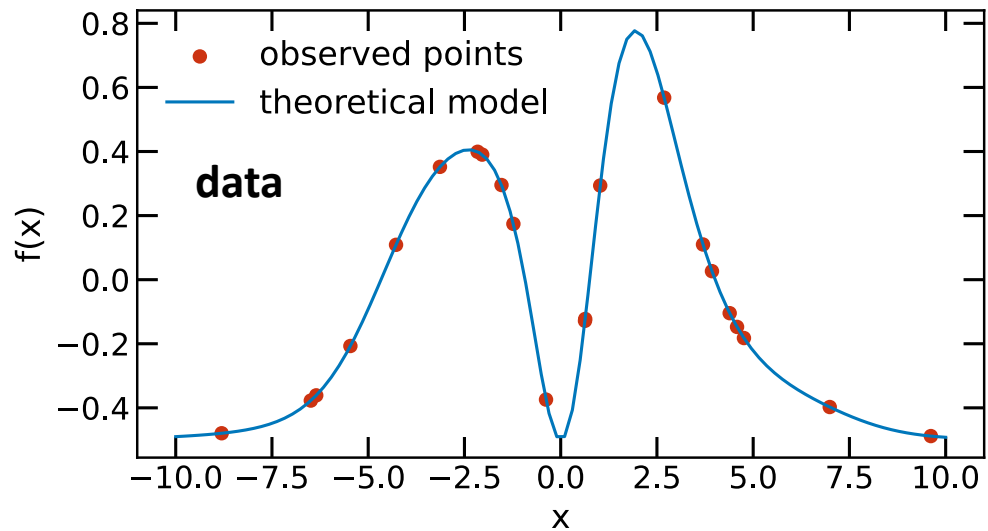
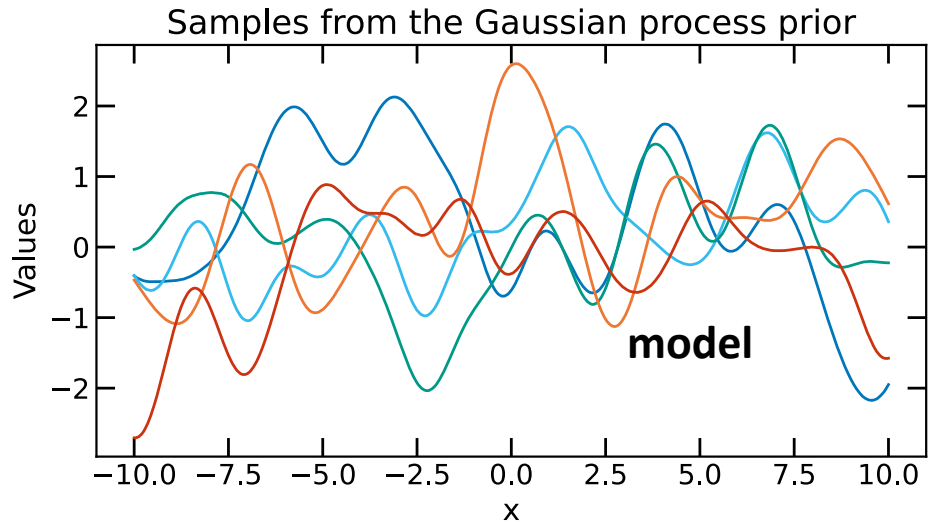
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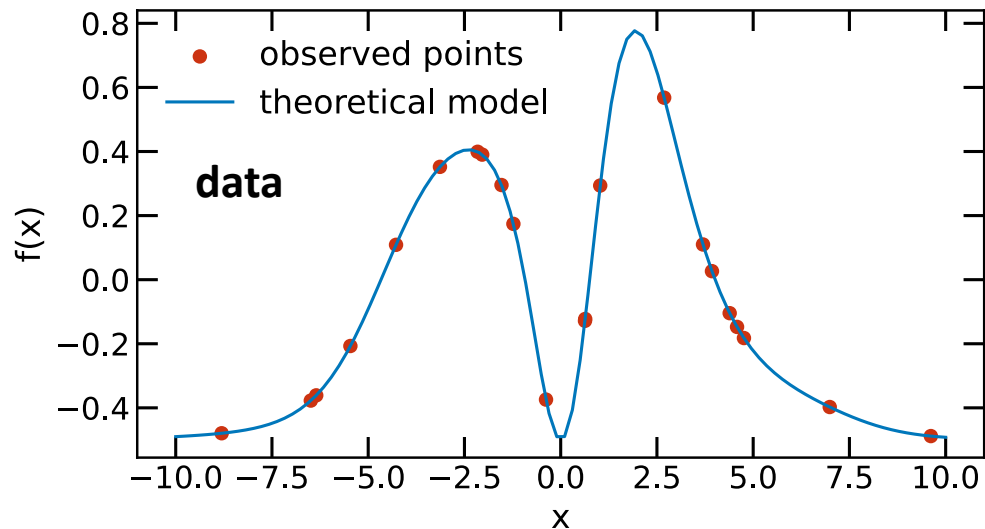
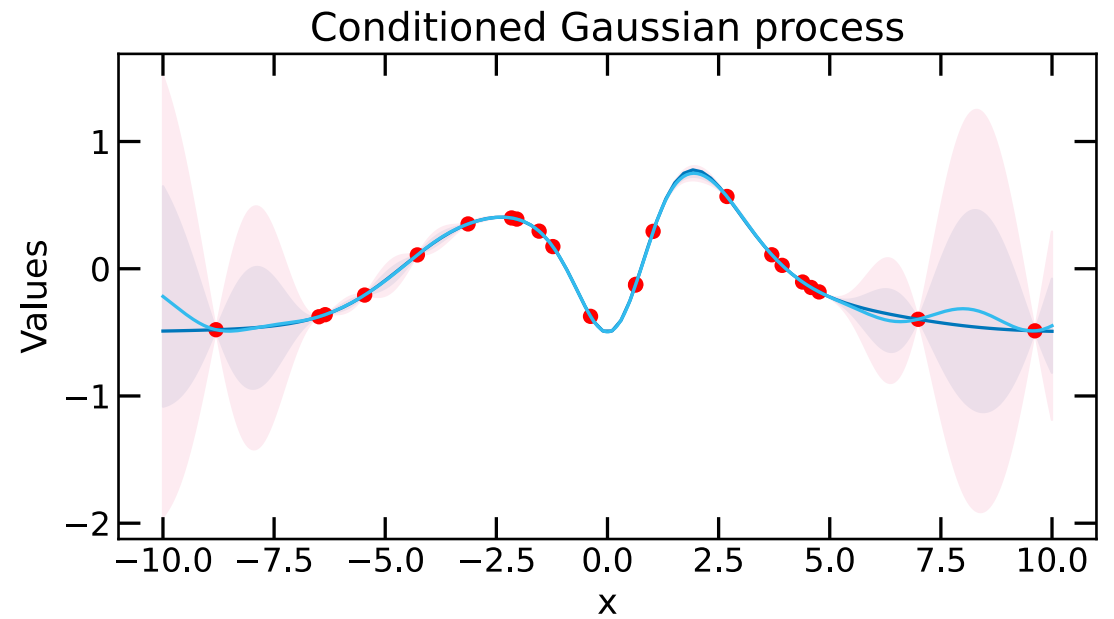
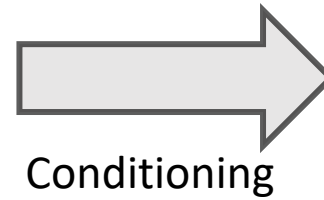
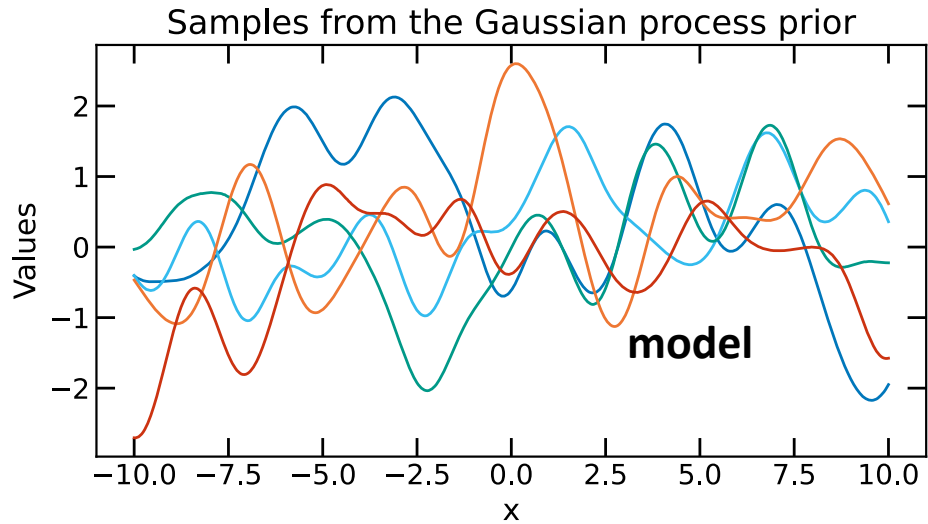
# Gaussian process regression

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# Gaussian process regression

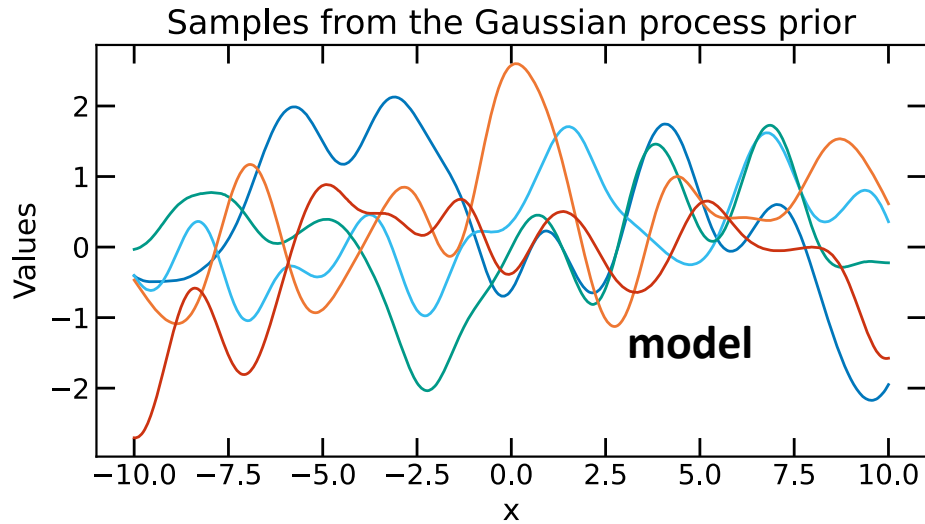
Rasmussen & Williams, 2006



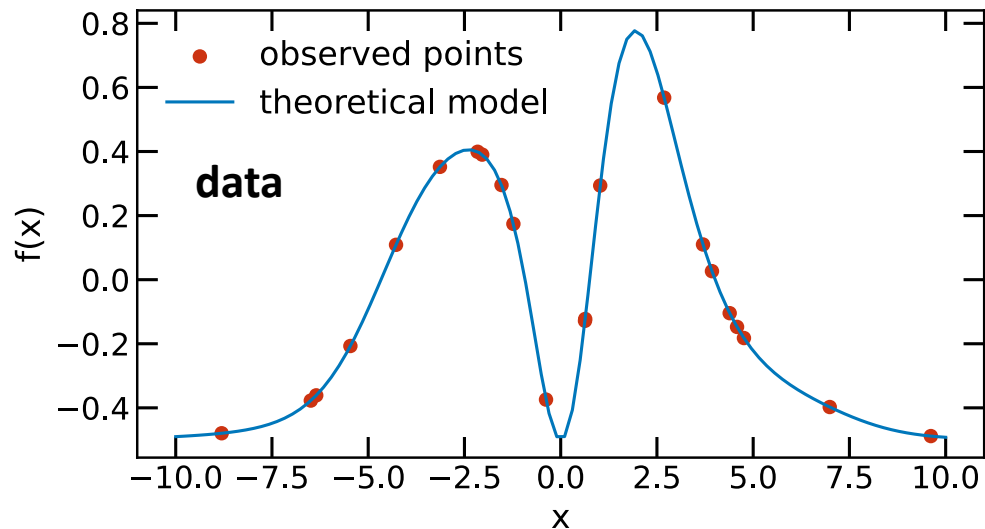
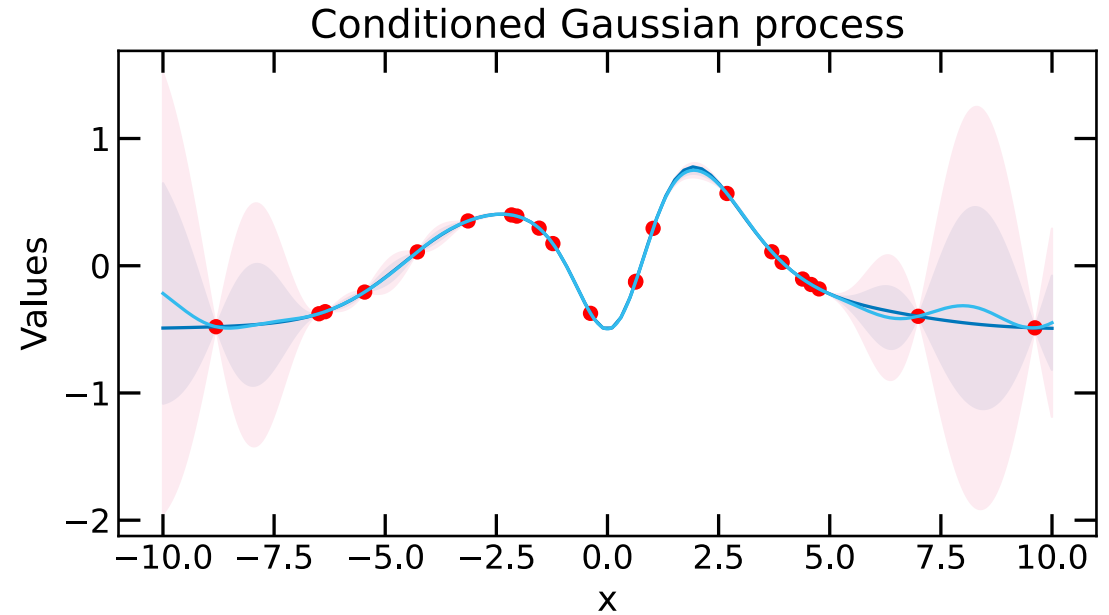


# Gaussian process regression

Rasmussen & Williams, 2006



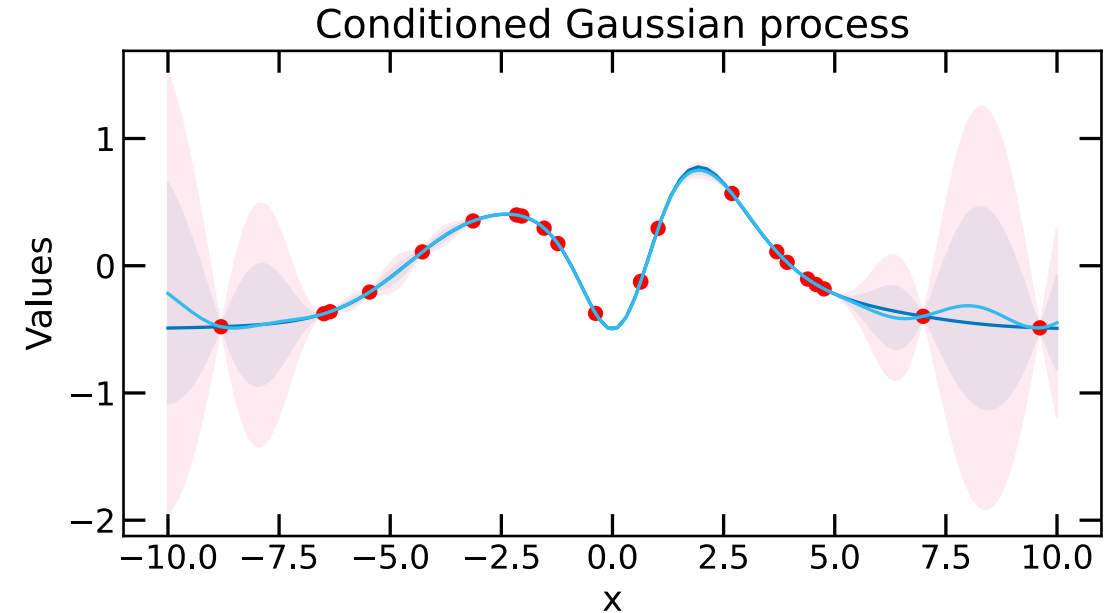
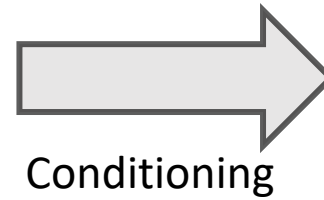
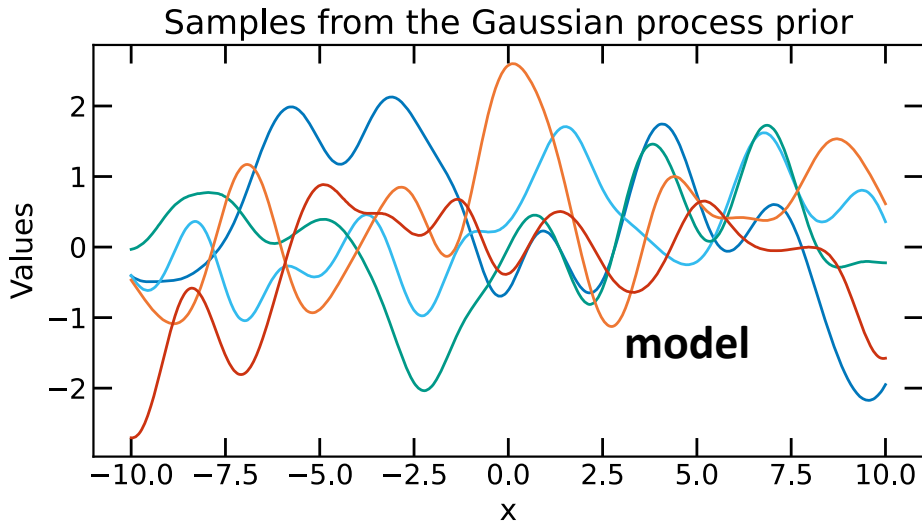
Conditioning



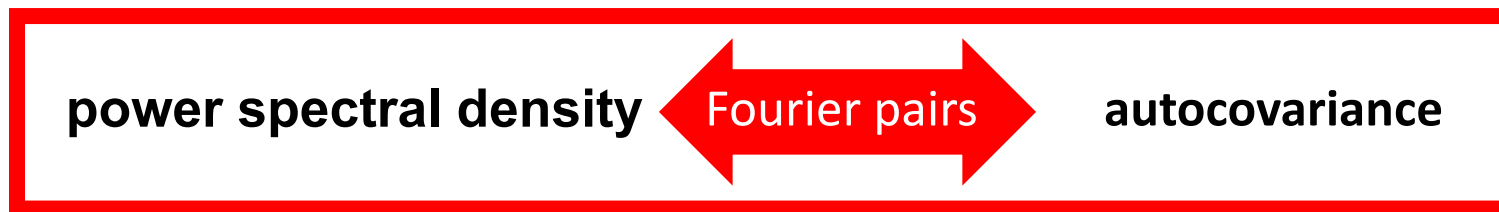
Then, we can find the set of best *hyperparameters* to interpolate the data.

# Gaussian process regression

Rasmussen & Williams, 2006



Then, we can find the set of best *hyperparameters* to interpolate the data.



Similar to

Miller+2010  
Zoghbi+2013

# Models for the power spectrum

- Analytical ACVF:

- Damped random walk  $P(f) \propto \frac{1}{1+f^2}$

CARMA process, Kelly+2014

- Celerite  $P(f) \propto \frac{1}{1+f^4}$

Foreman-Mackey+2017

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- Single bending power-law:  $P(f) = A \left(\frac{f}{f_b}\right)^{-\alpha_1} \frac{1}{1+\left(\frac{f}{f_b}\right)^{\alpha_2-\alpha_1}}$

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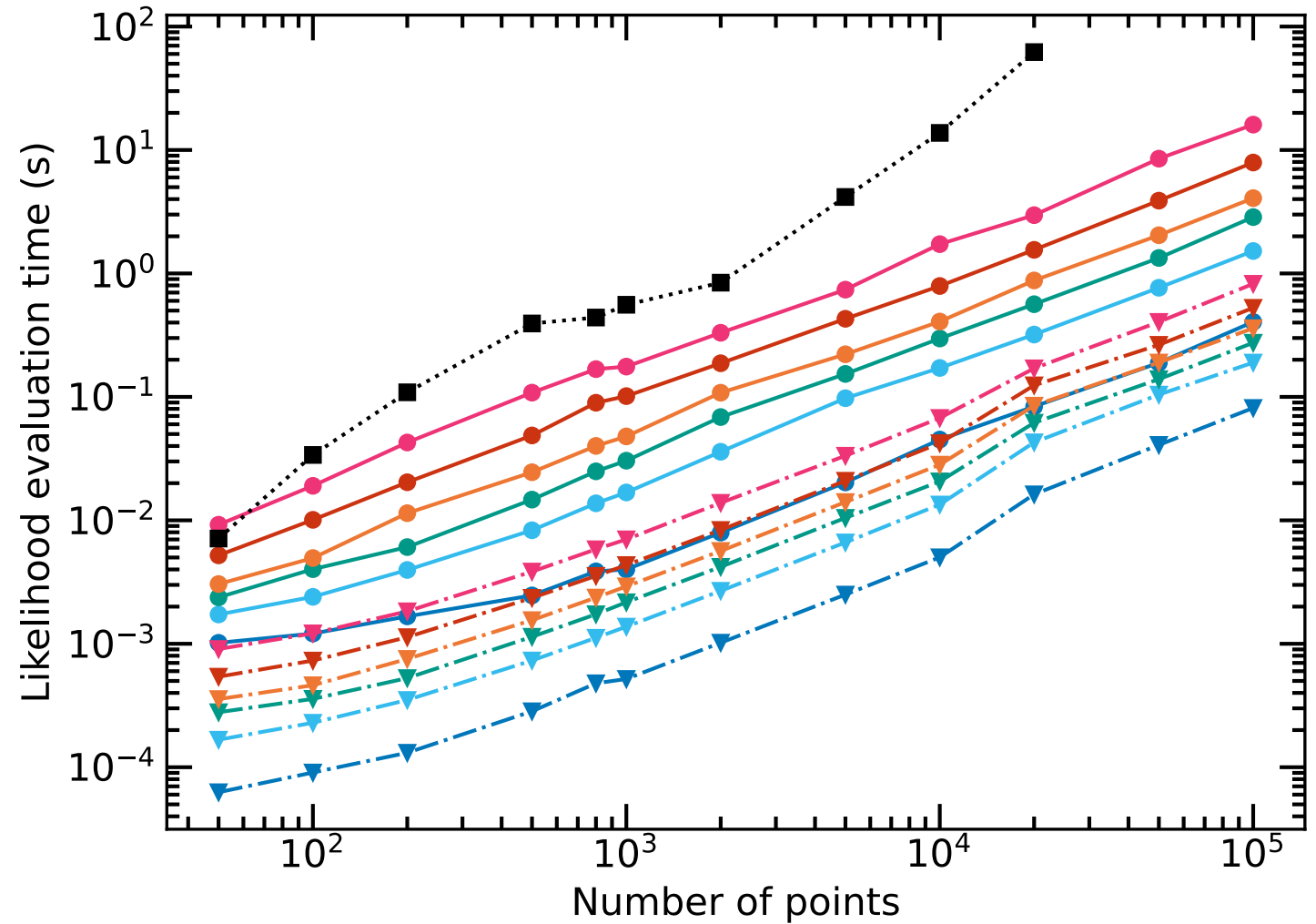
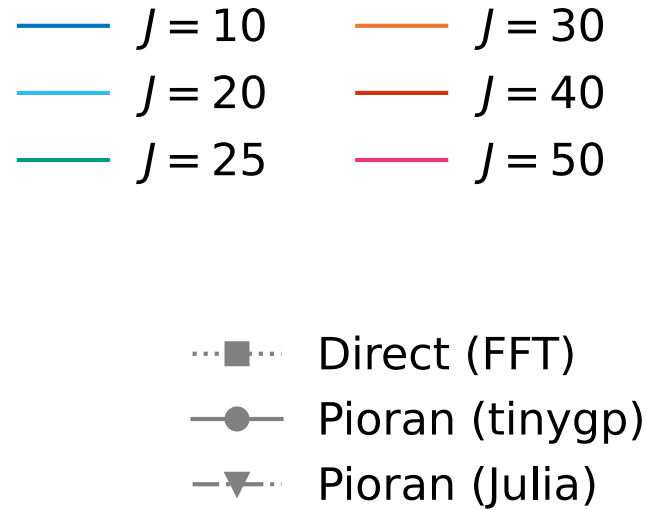
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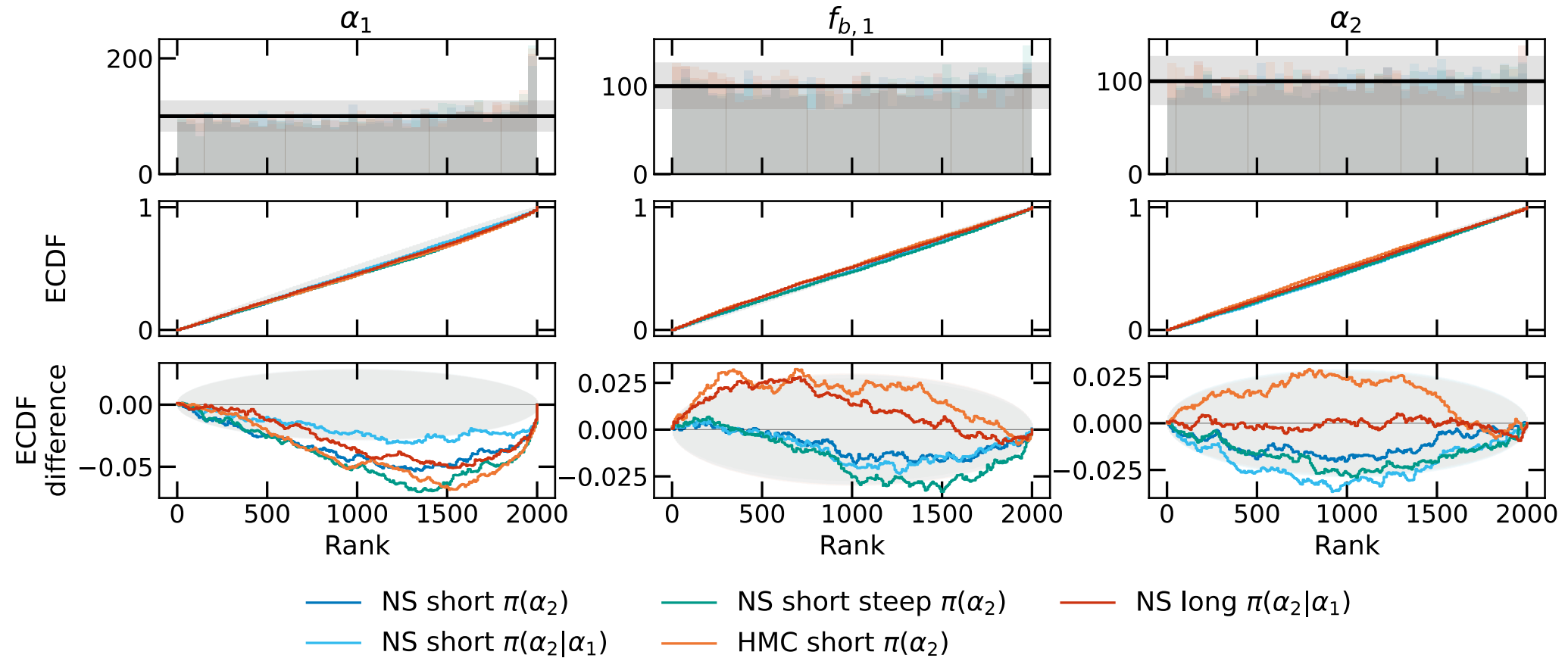
**Solution:** approximate the power spectrum with a sum of Celerite ACVF  
- likelihood computation scales as  $O(N J^2)$



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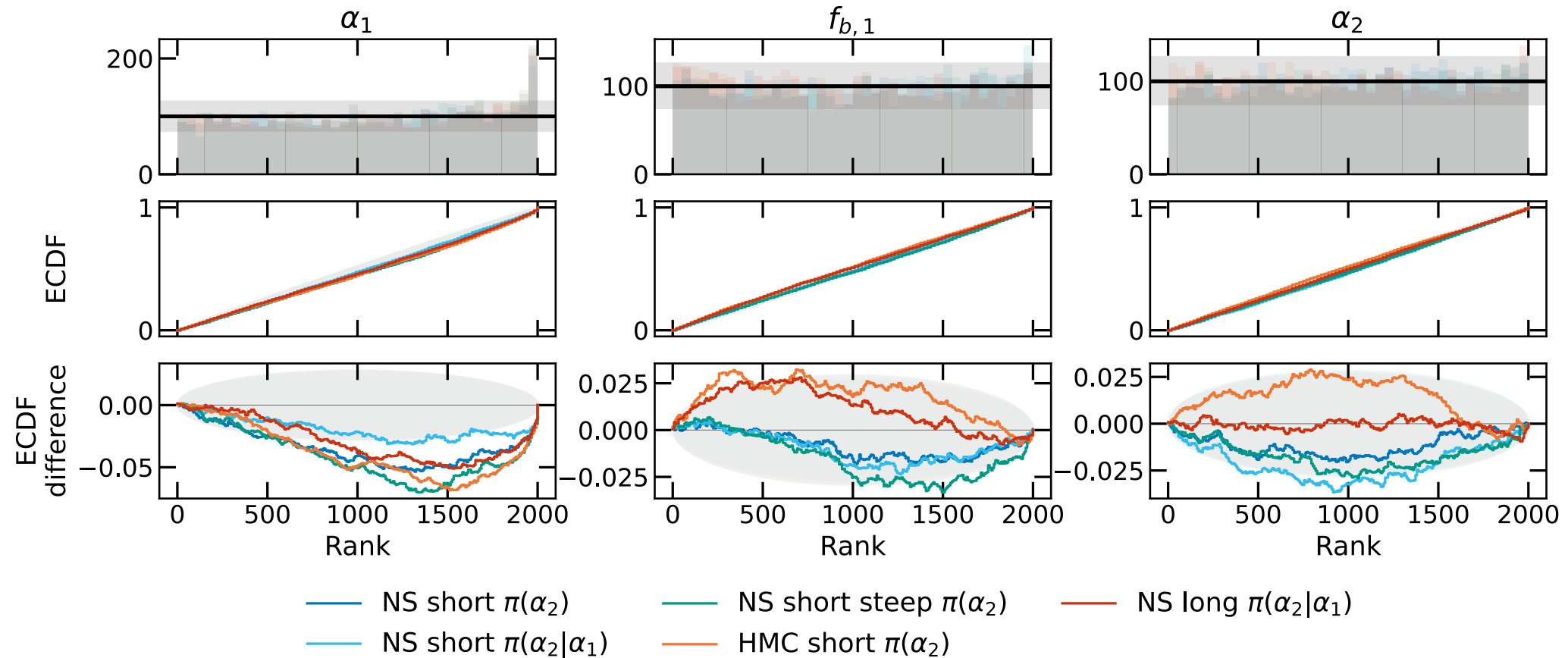
# Simulation-based calibration

Talts+2018, Säilynoja+2021



# Simulation-based calibration

Talts+2018, Säilynoja+2021



**Validation:** the method can correctly recover power spectrum parameters  
**but** the low-frequency slope can be **overestimated** if the bend frequency is too small



# About the non-linear variability of X-ray light curves and other assumptions

- We assumed Gaussian data



Lognormal process

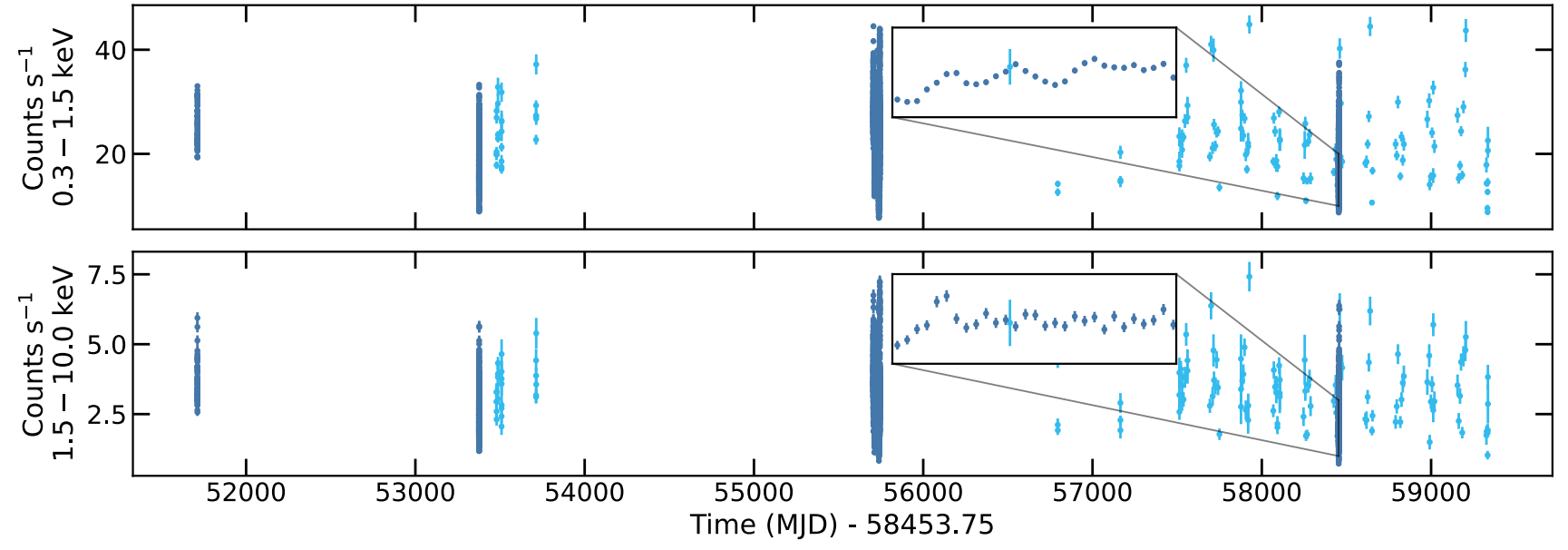
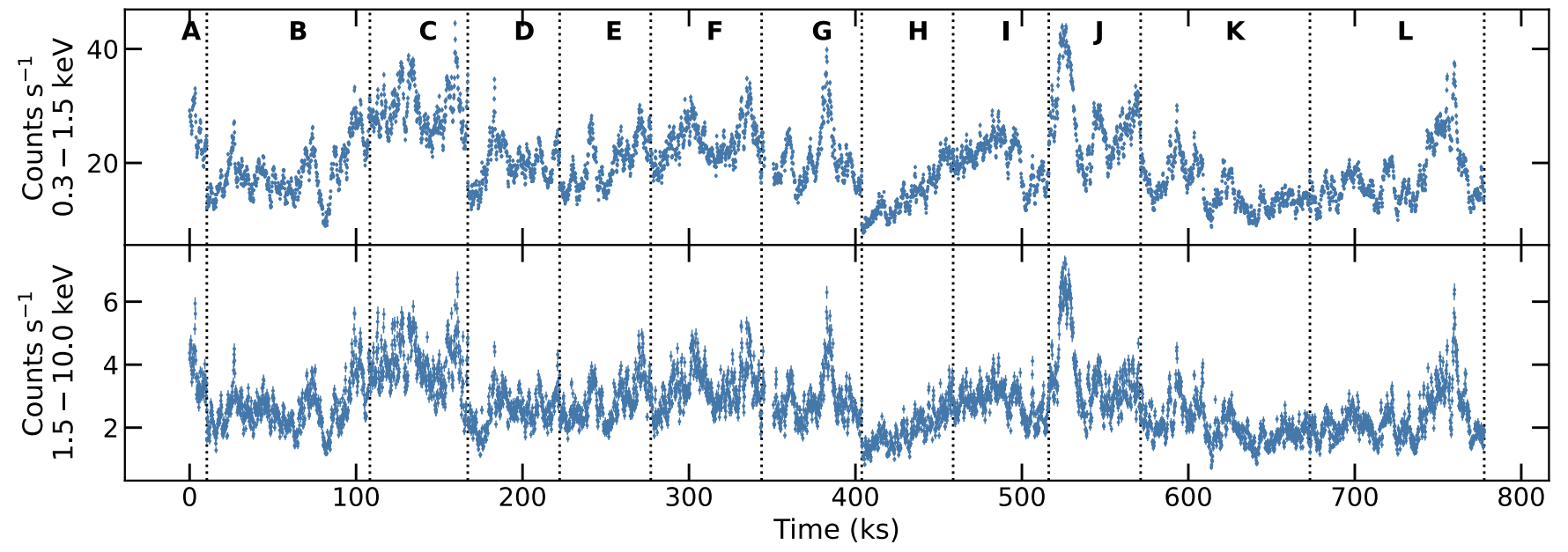
Uttley+2005

logarithm of  
the data

- We also assumed that the time series is weakly stationary

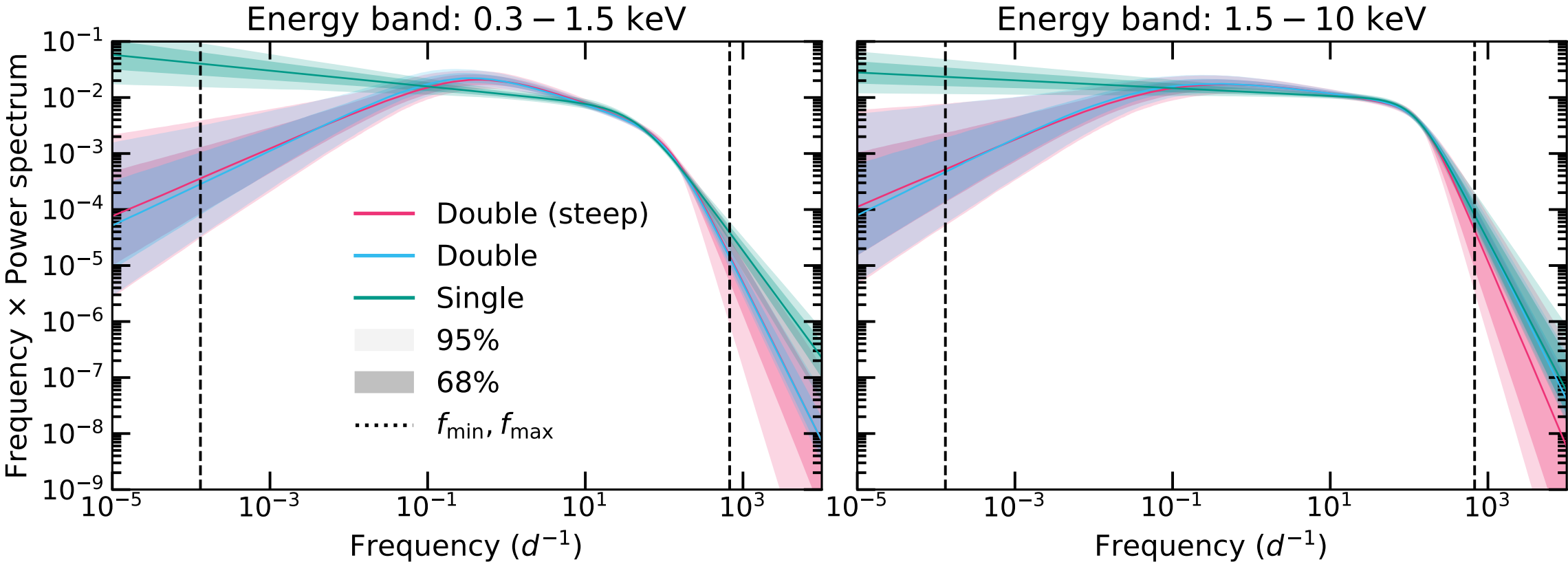
- In fact, it is sampled with a Poisson process (not implemented yet!)

# Ark 564 observed by XMM-Newton and Swift



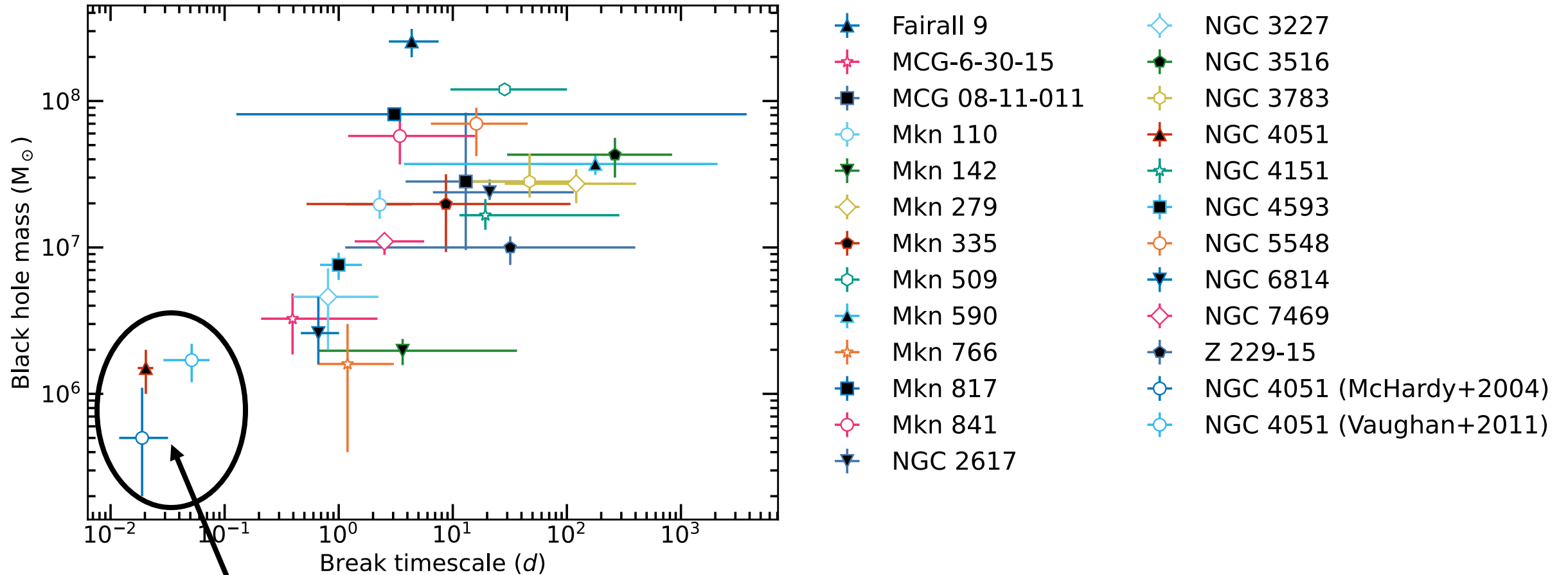
Swift XMM-Newton

# Revisiting the power spectrum of Ark 564



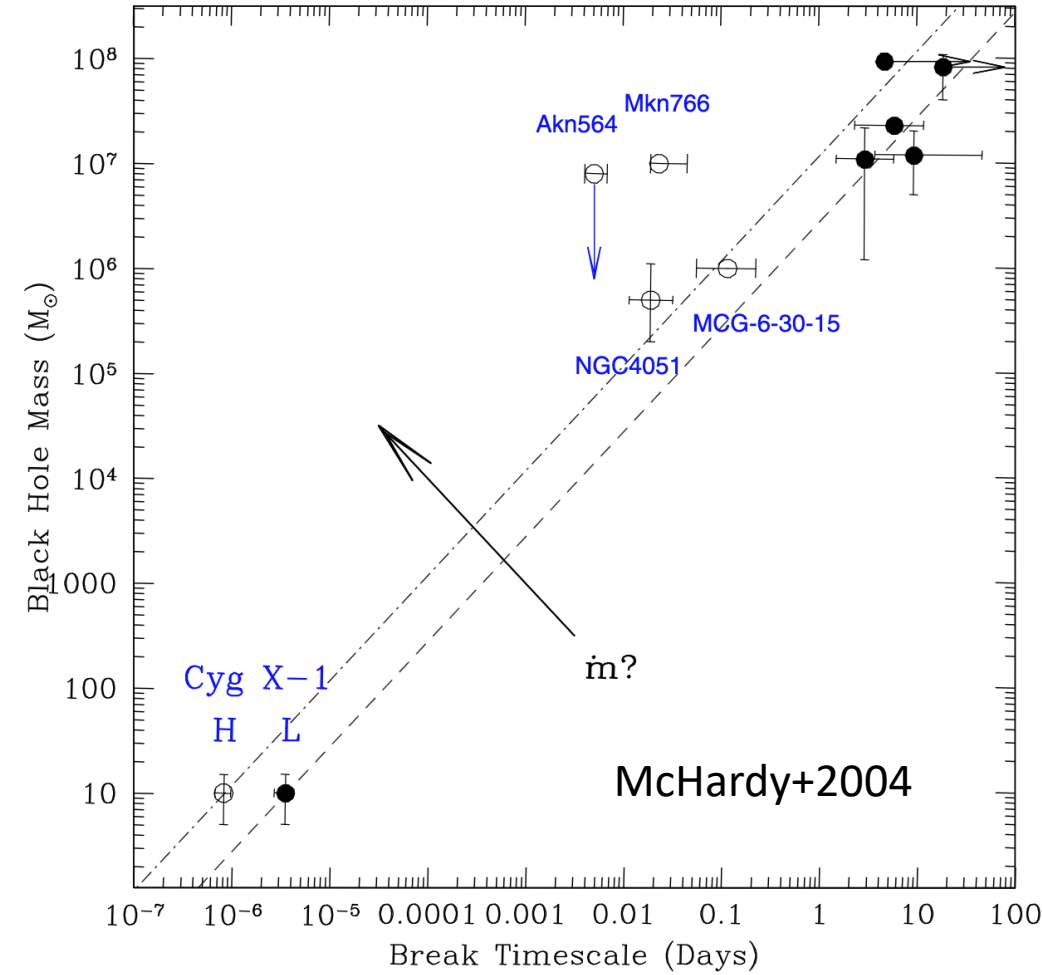
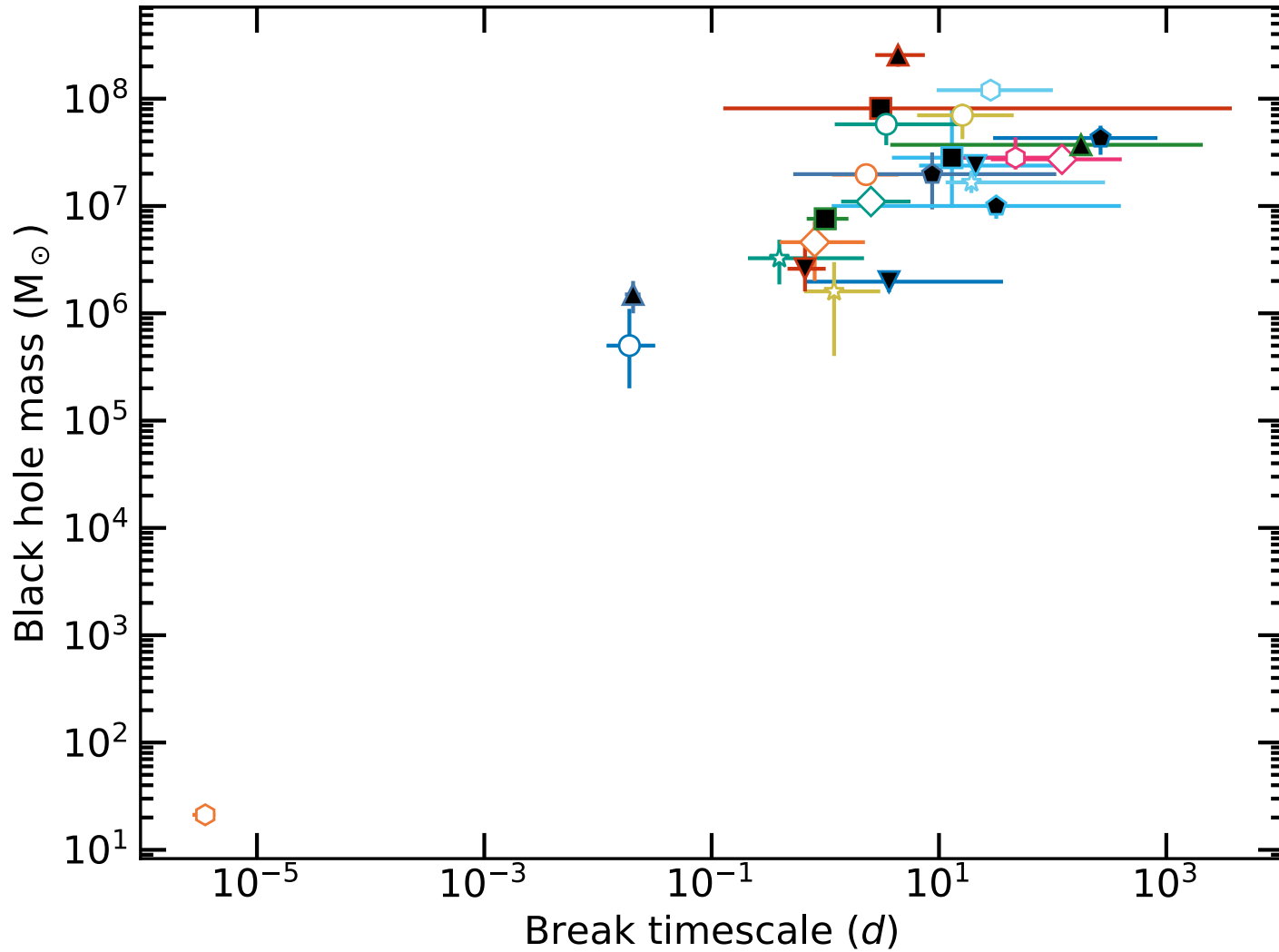
Results consistent with the works of McHardy+2007 using only Swift and XMM-Newton observations

# Break time scale – Black hole mass diagram – Work in progress!!

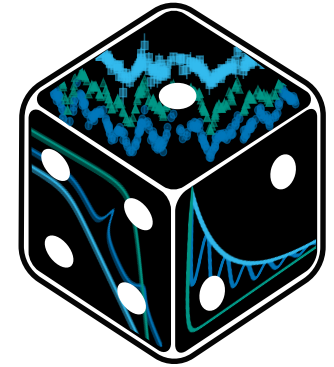


NGC 4051 using XMM-Newton observations

# Break time scale – Black hole mass diagram – Work in progress!!



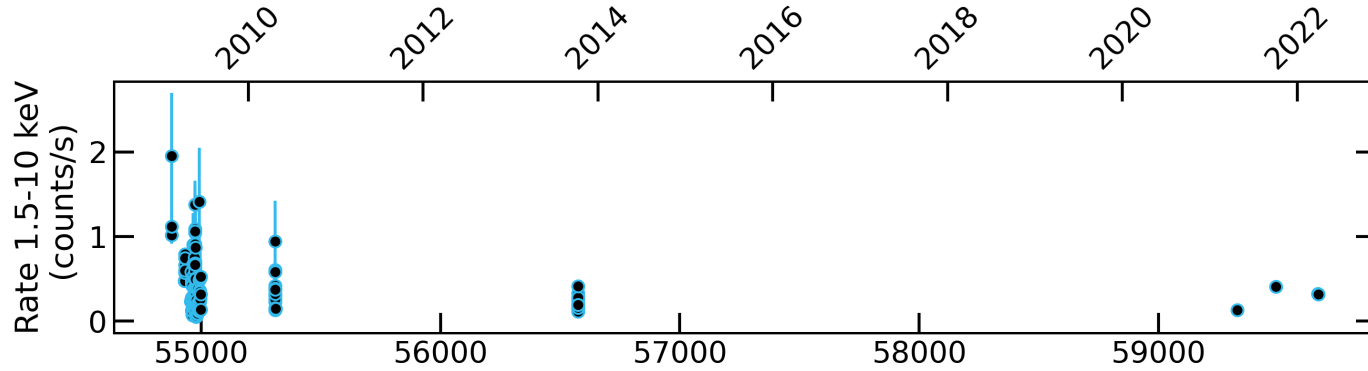
# Conclusions



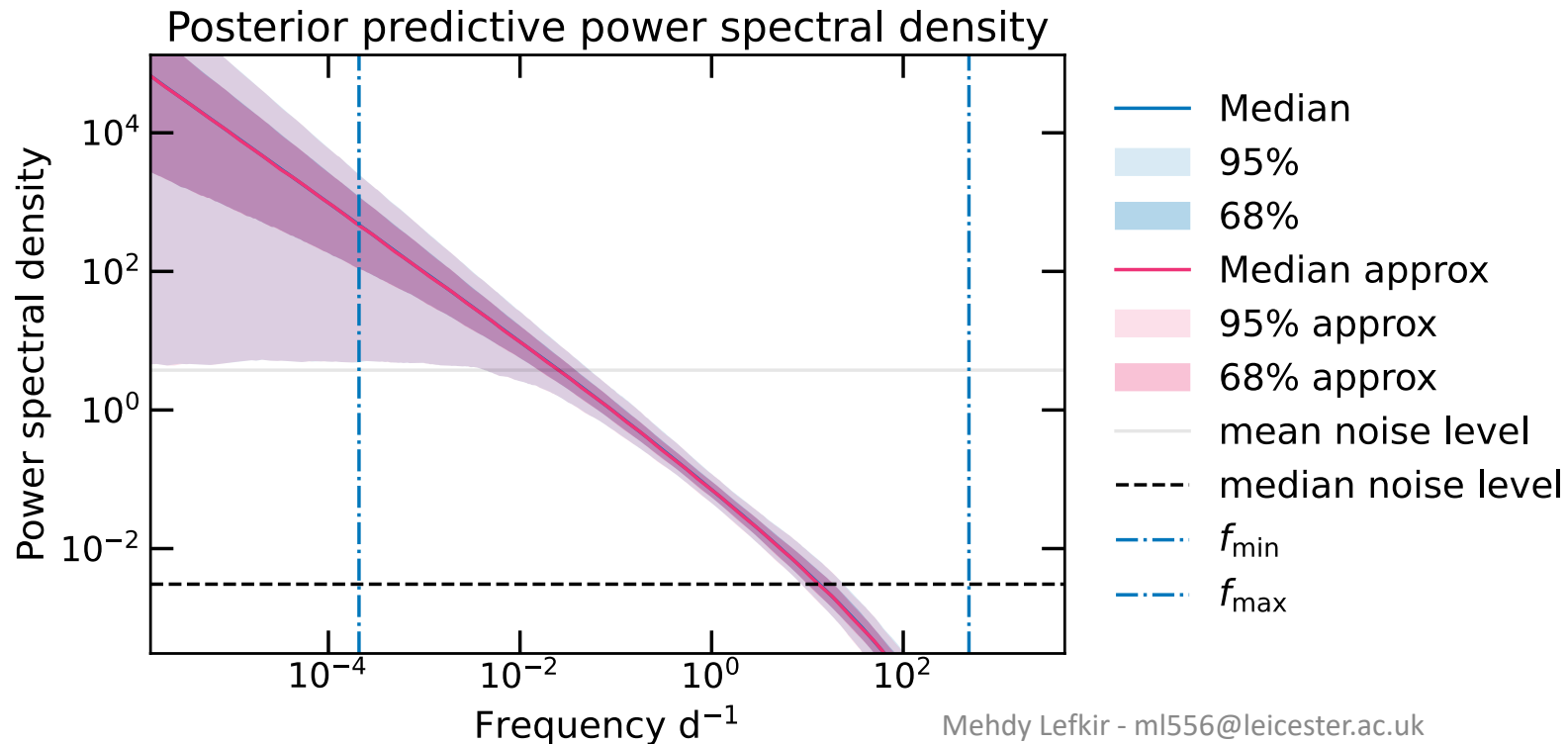
- We have a method to estimate the shape of the power spectrum:
  - Works on irregularly sampled time series
  - Validated with simulations
  - Scales on large datasets
  - Accounts for log-normal distribution
- With Julia and Python (JAX) implementations, currently being integrated in Stingray
- Paper describing the method under internal review
- Next steps:
  - Application to a sample of  $\sim 50$  AGN with RXTE and Swift+ XMM-Newton data
  - Correlations with other wavelengths, reverberation mapping

# NGC 4051 – a “low” mass AGN: with Swift

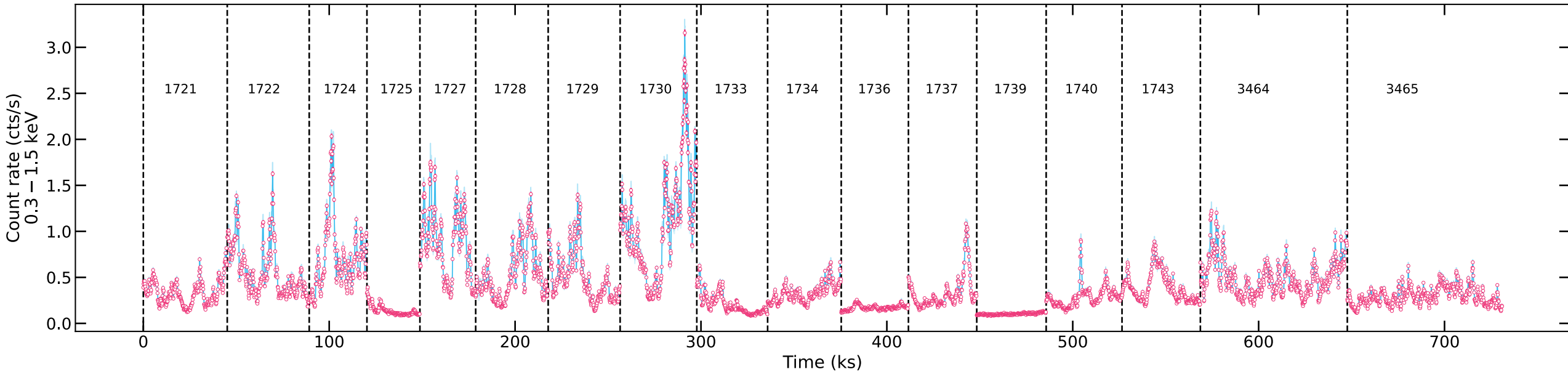
## NGC 4051



- fast variability difficult to see with Swift



# NGC 4051 – a “low” mass AGN: with Swift and XMM-Newton



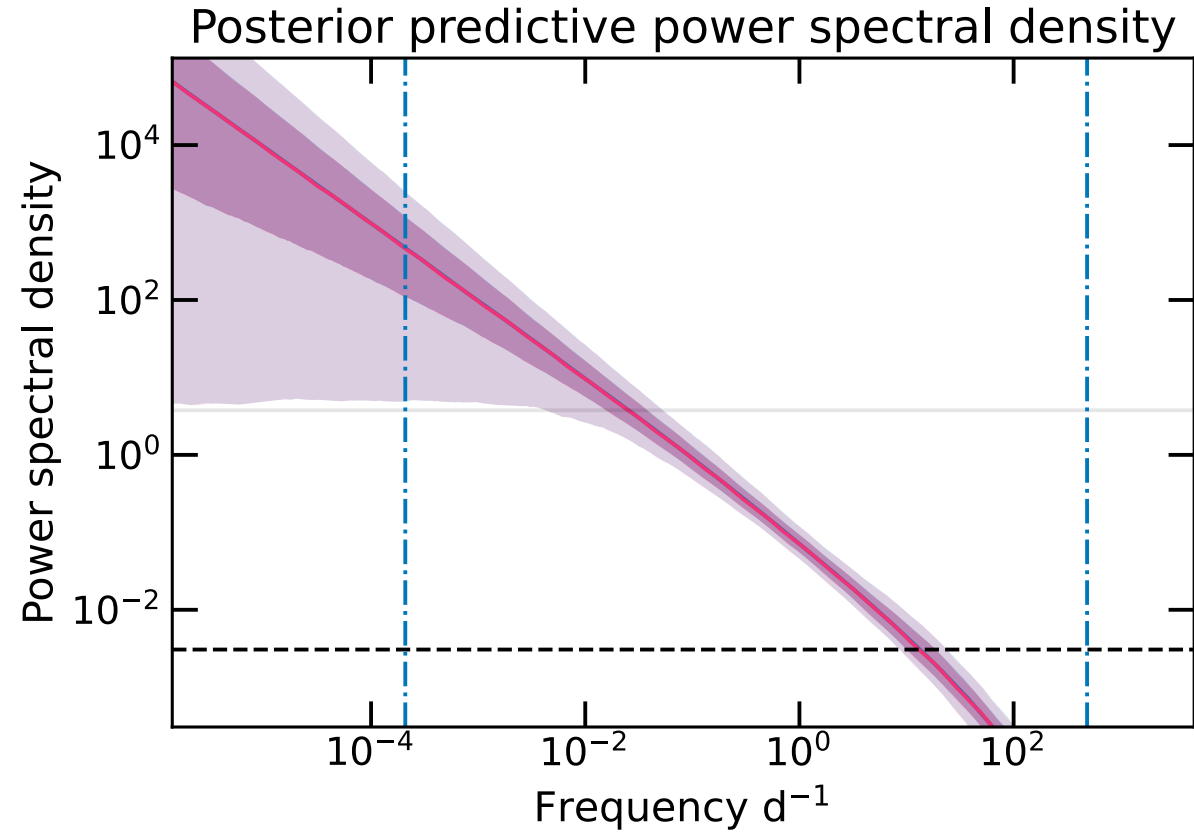
- About 5000 points!
- with a sampling period of 150s

Can we see the fast variability?

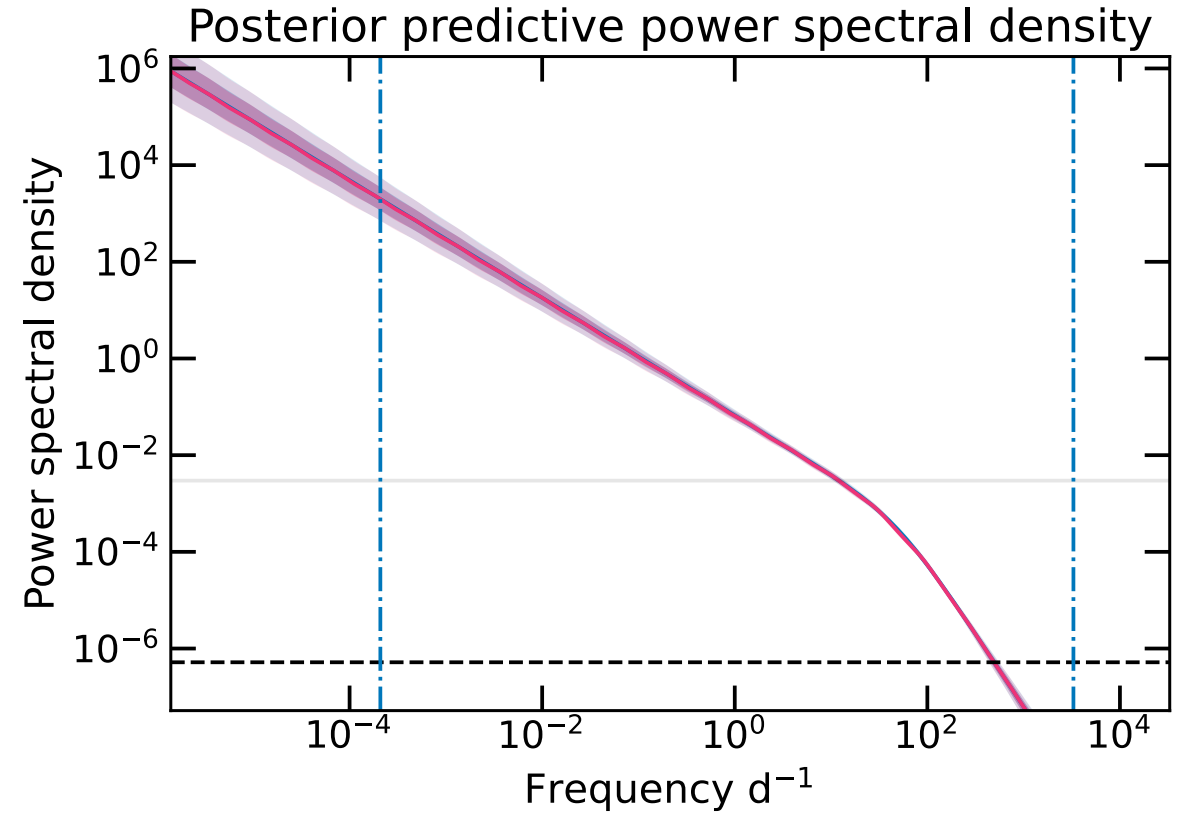


# NGC 4051 – a “low” mass AGN: with Swift and XMM-Newton

**Swift only**



**Swift and XMM-Newton**



# NGC 4051 – a “low” mass AGN: with Swift and XMM-Newton

